In your derivations, you may find useful the following approximate expansion:

$$(R + \Delta r)^3 \approx R^3 + 3R^2\Delta r, \text{ when } \Delta r \ll R. \tag{8}$$